RSFQ TECHNOLOGY: CIRCUITS AND SYSTEMS

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Rapid Single-Flux-Quantum (RSFQ) logic is a superconductor IC technology that, with only a modest number of researchers worldwide, has produced some of the world's highest performance digital and mixed-signal circuits. This achievement is due, in part, to a constellation of characteristics that manifest themselves at the circuit level – namely, high-speed digital logic at low-power, ideal interconnects, quantum accuracy, scalability, and simplicity of fabrication. A necessary key to translating these advantages to the system-level involves understanding the I/O, synchronization, and packaging issues associated with a cryogenic technology. The objective of this paper is to review the status of current RSFQ circuit-level infrastructure components and their potential impact on system-level applications.

1. Introduction

As the RF and digital domains converge¹, entirely new strategies are needed to enable the innovative applications that will drive tomorrow's electronics industry. The ability to deploy 100+ GHz mixed-signal systems will usher in a telecommunications and computer revolution. Specific areas to benefit include:

► The wireless communications industry – Given the insatiable "thirst for bandwidth" in digital telecommunications, future data converters and digital signal processors will be required to deliver greatly increased performance to meet the connectivity demands of governments, businesses, and consumers.

► The defense/government market – The never-ending drive for militaries and governments to do "more with less" is resulting in a concentrated push to deploy multifunction, dynamically reconfigurable systems. Such systems will rely on flexible, ultrafast, digital technologies, and replace, consolidate, and expand the capability of existing dedicated analog systems for radar, electronic warfare, and other surveillance applications.

► The hyper-computer business – Demand for access to intensive computation for weather prediction, non-invasive geo-physical exploration of natural resources, global economic modeling, intensive data mining, and other applications already exceeds the abilities of modern supercomputers and networks. Ever-faster processing capabilities, ultra-low latency memories, and ultra-high throughput network switches will be needed.

For traditional three-terminal semiconductor transistor devices, a cutoff frequency f_{max} approaching 1 THz is needed to achieve a throughput on the order of 100 Gb/s for small application specific ICs (ASICs).² Such performance requirements are beginning to reach the limits of the physical properties of semiconductors.^{3,4}

Further, it has been noted that the rate of innovation in semiconductor materials and devices has slowed dramatically, and that virtually no improvement in device speed is anticipated beyond the next five years.⁵ Ultra-exotic or "speculative" technologies such as quantum computing⁶, DNA⁷ and molecular computing⁸ represent a paradigm shift unthinkable until, at the earliest, the middle of the century. To sustain the historical performance growth in the electronics industry, a radically new IC technology – one that is scalable and addresses the problems of both device speed and interconnect delay – must be identified and nurtured, while keeping cost in mind. RSFQ technology, based on low-temperature superconductors⁹, could be the answer.

Rapid Signal Flux Quantum (RSFQ) logic¹⁰ is an IC technology with the potential to leapfrog the performance of traditional silicon and III-V compound semiconductors. ICs with sub-micron RSFQ static digital frequency dividers have already been fabricated and operated in university laboratories at over 750 Gb/s.¹¹ These achievements represent faster demonstrated electronic circuit speeds than any other technology has predicted to date, even through computer simulations. Prototype RSFQ circuits made with modest research-grade 2-3 μ m linewidth niobium (Nb) fabrication processes have demonstrated circuits such as those shown in Table 1.

Circuit Type	Circuit metric(s)	Circuit Type	Circuit metric(s)
Toggle flip-flop	144 GHz	2-bit counter	120 GHz
4-bit Shift register	66 GHz	1-kbit shift register	19 GHz
6-bit <i>Flash</i> analog-to- digital converter (ADC)	3 ENOB ^a at 20 GHz	6-bit Transient digitizer with 6×32 bit on-chip memory buffer	16 GS/s
14-bit High-resolution ADC (2 MHz)	14 ENOB & -100 dBc SFDR ^b	19-bit Digital-to-analog converter	fully functional at low speed
1:8 Demultiplexor (synchronous)	20 Gb/s	1:2 Demultiplexor (asynchronous)	95 Gb/s
1-bit Half-adder	23 GHz	2-bit Full-adder	13 GHz
8×N bit serial multiplier	16 GHz	14-bit digital comb filter	20 GHz
128-bit autocorrelator	16 GHz	Time-to-digital converter	31 GHz

Table 1: Representative RSFQ circuits demonstrated in 2-3 µm Nb technologies.

^a ENOB =effective number of bits

^b SFDR *spurious-free dynamic range*

The RSFQ technology also has a clear path to extend performance. Unlike semiconductor devices, the speed of RSFQ ICs comes from inherent physical

phenomena, not ultra-small scaling. This means that existing lithography techniques can be employed, and more importantly, existing equipment can fabricate circuitry that surpasses conventional limits of performance. Because RSFQ logic uses the lossless ballistic transmission of digital data "fluxons" near the speed of light, the wire-up nightmare that silicon designers face is substantially reduced. This scenario also allows the full speed potential of individual gates to be realized.

Other features of this technology that make it suitable for growth into the traditional market include its compatibility with existing IC packaging techniques. These include compatibility with optical (fiber) signal input and output, a maturing multi-chip module (MCM) technology with multi-Gb/s digital data transfer between chips, and simple interface circuits to convert to and from both ECL logic and CMOS logic levels.

RSFQ integrated circuits are made with standard semiconductor manufacturing equipment; however, there are many fewer mask layers (typically about 10) and the actual processing involves much less complex depositions.^{12,13} Because RSFQ logic is an all thin-film technology, there are no doping profiles to calculate, no high-temperature drive-ins, no epitaxial growths or chemical-vapor depositions. These differences translate directly into reduced costs in the large-scale manufacture of RSFQ electronics.

System-on-a-chip (SOC) architectures, containing both front-end analog circuitry, as well as digital processing blocks, are fundamental to enabling tomorrow's 100 GHz applications. This configuration presents extraordinary difficulties for semiconductors, due to "crosstalk" – problems of interference between the analog and digital sections of the same chip. Because of the unique reliance on single quanta of magnetic flux to convey information, RSFQ are inherently more immune to this sort of crosstalk.

1.1 Development of the Rapid Single Flux Quantum IC Technology

The existence of the magnetic flux quantum in a superconductor circuit was first predicted in 1950 by Fritz London.¹⁴ In 1961, Bascom Deaver and William Fairbank were able to experimentally prove this theory in their laboratories at Stanford University (Palo Alto, CA).¹⁵ The postulation and subsequent discovery of an active superconductor device—the Josephson junction¹⁶—in 1962 quickly led to a number of efforts to exploit the speed and power advantages of a circuit made from a resistanceless (superconductive) material; however, virtually all of these ideas sought to copy the voltage-level output of the transistor, and its predecessor, the vacuum tube.¹⁷ Called Josephson "latching logics", perhaps, the most notable of these development efforts was the superconducting supercomputer program that ran from 1969-1983 at IBM (Yorktown Heights, NY).¹⁸

Ironically, about the same time IBM terminated its Josephson computer project, innovative solutions were being found to design problems that had plagued the latching logic approaches. As a result, modern RSFQ logic as a digital superconductor technology differs from this original latching junction work in three fundamental ways: junction material, logic convention, and packaging. These advances were a result of work in a number of laboratories and countries and are summarized in the following sections.

1.1.1 Use of refractory metals – niobium

Nb RSFQ ICs tolerate thermal and mechanical environments well, unlike previous Pballoy Josephson circuits, which did not endure the environmental stresses of ordinary use.

By the early 1980s, it had become clear that a better material system and more rugged Josephson IC process was needed. At the Sperry Research Center (Sudbury, MA), Harry Kroger, Larry Smith, and Don Jillie introduced what is now known as the "trilayer process", a method of creating reproducible superconducting tunnel barriers across a wafer.¹⁹ Using this trilayer approach, a stable Nb/Al Josephson junction process was developed at Bell Laboratories (Murray Hill, NJ) by Michael Gurvitch, John Rowell and others.²⁰ This Sperry/Bell Labs "Nb/Al trilayer process" is now used universally to make Nb RSFQ ICs and other superconductor devices, such as sensors that measure the magnetic fields from the heart and brain. The next step in the development of the modern RSFQ fab process was made in Japan, where, in a Ministry of International Trade and Industry (MITI) funded project, researchers at Fujitsu, Hitachi, NEC, and Japan's Electrotechnical Laboratory (ETL) showed how the Nb/Al trilayers, which initially were used in the US to make only small numbers of junctions, could be developed into a complete fabrication process for complex Josephson ICs.^{21,22,23} The junction count in such ICs is, in principle, limited only by the available lithography and wafer size. Since the 1980s there has also been progress, particularly at TRW (Redondo Beach, CA), and at ETL (Japan) in replacing the Nb/Al trilayer process with one that uses NbN as the superconductor, allowing operation at somewhat higher temperatures (~10 K);²⁴ however, the majority of R&D in the field worldwide remains based on the Nb/Al process.

1.1.2 Magnetic flux quanta as binary data

RSFQ logic does not try to mimic semiconductor voltage-level logic, as did the Josephson latching-logic schemes (which incidentally suffered from the same speed restrictions of a few GHz that today's semiconductor digital VLSI logics are encountering).

During the mid-1980s, a group of researchers at Moscow State University (Moscow, Russia), including Konstantin Likharev, Oleg Mukhanov and Vasili Semenov, invented a new Josephson junction logic family tailor-made to access the ultimate potential of superconductors. This new superconductor digital logic family became known as Rapid Single Flux Quantum (RSFQ) logic.^{25,26} (see also Ref. 10) This approach relies on another intrinsic property of superconductors (apart from the loss of resistance below a critical temperature T_c), namely that within a closed section of superconductor material any magnetic flux present can exist only in discrete amounts that are multiples of the magnetic flux quantum, $\Phi_0 = h/2e \approx 2.07 \times 10^{-15}$ Wb, where *h* is Planck's constant and *e* is the electron charge (i.e., it is said to be quantized).²⁷ When a flux quantum moves in an electrical circuit, it is manifested as a fast voltage pulse – an "SFQ pulse" – with an integrated amplitude of $\int V(t) dt = \Phi_0 \approx 2.07$ mV-ps. Use and manipulation of single quanta of magnetic flux, in superconducting devices called "flux shuttles", was first demonstrated in 1971 by Philip Anderson, Robert Dynes, and Ted Fulton of Bell Laboratories (Murray Hill, NJ).²⁸ Another such logic scheme was proposed in 1978 by John Hurrell and Arnold Silver at the Aerospace Corporation (Los Angeles, CA).²⁹ At the same time in Japan, a group at Tohoko University was developing what would become known as "phase-mode logic".^{30,31} Although all are based on SFQ pulses, none of these approaches adequately defined a convenient manner for coding binary data onto and extracting it from the magnetic flux quanta in the circuit. A primary contribution of the RSFQ approach was to define a convention for the logical representation of single flux quantum "1"s and "0"s. This made RSFQ a synchronous (clocked) logic, departing from the traditional combinatorial Boolean logic style. Since the mid-1980s, a number of other logic families utilizing SFQ pulses have been proposed^{32,33,34}, including dual-rail or "delay-insensitive" gates. Nevertheless, the RSFQ convention for performing digital and mixed-signal logic with superconductors has now become the dominant approach among researchers around the world.

1.1.3 Availability of closed-cycle refrigeration

RSFQ circuits also no longer have to rely solely on liquid-helium cooling, as did their previous voltage-state counterparts. Modern commercial closed-cycle cryogenic refrigerators ("cryocoolers") make packaging RSFQ chips manageable and comparably inexpensive. Such refrigerators can cool the niobium superconductor chips to their operating temperature of 4-5 K. Although this cooling is often accomplished with liquid helium (LHe) in research laboratories, cryocoolers are almost always the best packaging choice for commercial or military systems. Over the past decade, the reliability and efficiency of such cryocoolers has improved, while their size and cost has decreased.³⁵ In fact, it is now possible to purchase a cryocooler that reaches 4-5 K, and fits in the lower half of a standard 19 in. instrument rack, for about us\$20,000.³⁶ Further improvements and cost reduction, particularly of pulse-tube refrigerators³⁷, seems likely.

1.2 Contents of this review

This article gives a general overview of the RSFQ technology at the circuit and system level. It is intended to serve as a companion paper to "RSFQ Technology: Physics and Devices" by Paul Bunyk, Konstantin Likharev, and Dmitry Zinoviev (also in this issue), which covers, in detail, the theoretical underpinnings, basic operation, and possible future directions of RSFQ technology. This review is confined to work in low-temperature superconductor (LTS) development of RSFQ circuits in Nb/Al trilayer material systems. Recent advances in device/circuit research on RSFQ and digital gates in high-temperature superconductor (HTS) materials can be found in Ref. 38. Work in NbN/MgO and NbN/AlN material systems is covered in Refs. 22 and 39 respectively. Reviews of the status of the commercialization of superconducting electronics in general can also be found in the literature.^{40,41,42}

After originating at Moscow State University (Moscow, Russia), the majority of LTS RSFQ circuit work was performed, over roughly the last 10 years, at the following US institutions: HYPRES, Inc. (Elmsford, NY); Northrop Grumman (Baltimore, MD); TRW (Redondo Beach, CA); NIST (Boulder, CO); Conductus (Sunnyvale, CA); University of Rochester (Rochester, NY); Stanford University (Palo Alto, CA); UC Berkeley (Berkeley, CA); MIT Lincoln Laboratory (Lexington, MA); and SUNY Stony Brook (Stony Brook, NY).

More recently, a number of major institutions in Japan have stepped up their involvement in the design and development of Nb RSFQ circuits and systems. These include: NEC Fundamental Research Laboratories (Tsukuba, Ibaraki); Hitachi Advanced Research Laboratory (Kokubunji, Tokyo); Fujitsu Laboratories Ltd. (Atsugi-shi, Kanagawa); Tohoku University (Aoba-ku, Sendai); Nagoya University (Chikusa-ku, Nagoya); the University of Tokyo (Meguro-ku, Tokyo); Yokahama National University (Hodogaya-ku, Yokahama); the Electrotechnical Laboratory (ETL) (Tsukuba, Ibaraki); and the Superconductivity Research Laboratory (SRL) of the International Superconductivity Technology Center (ISTEC) (Koto-ku, Tokyo).

In Europe, the focus has continued to be more on HTS materials; however, LTS RSFQ work is also ongoing at the Technische Universität Ilmenau, (Ilmenau, Germany), the Physikalish-Technische Bundesanstalt (PTB), (Braunschweig, Germany), Chalmers tekniska högskola (Goteborg, Swedsen) and (on a small level) at Ericsson Components AB (Stockholm, Sweden).

This article is intended to outline the current state of a number basic circuit-level "building blocks" and techniques, developed by the above groups and others, which could be applied towards creating fully-functional RSFQ-based systems.⁴³ Section 2 covers advances in circuits for data conversion between analog and digital formats. Section 3 introduces digital signal processing core components such as adders and multipliers and other infrastructure components, such as clocks and data buffers. Section 4 focuses on clock and data input/output techniques, which become especially important due to both the high-speed and cryogenic nature of the technology. Finally, section 5 examines several integrated RSFQ applications and their system-level benefits, and gives a summary of promising development areas.

2. RSFQ Data Converters

The quantum accurate periodic transfer function of the Superconducting Quantum Interference Device (SQUID) makes superconductor circuits an obvious choice for data conversion from a continuous-time to discrete-time format.⁴⁴ Likewise, when a quantized SFQ pulse is used to represent digital data, the AC Josephson effect ²⁴ (i.e. frequency-to-voltage relationship)⁴⁵ gives access to a method for directly transferring back into the analog domain. RSFQ analog-to-digital converters (ADCs) have been one of the best-funded research areas in the field, since they offer both high-speed and high-fidelity performance. Digital-to-analog converters (DACs) have also received considerable

attention, since the basis for their operation is already commercially employed to define the SI (*Systeme Internationale*) unit of the Volt.⁴⁶ Several of the major efforts in these areas are discussed in the following sections.

2.1 Analog-to-digital converters

This interest in RSFQ ADCs is partly because of potential dual-use applications in civilian markets, such as software-defined radio, and to defense radar and EW systems. The fact that the performance of semiconductor ADCs has improved at an average rate of only ~1.5 bits per 6 years is a further stimulus. The performance of traditional semiconductor ADCs has been summarized by Robert Walden of HRL Laboratories (Malibu, CA)⁴⁷, and is plotted in Fig. 1. The overlaid data points for two fully functional RSFQ ADCs on this plot show demonstrated performance that is already comparable with the very best semiconductor devices. A number of different RSFQ ADC approaches have received attention, each design typically focussed on stressing different performance parameters. Among them are the HYPRES "high-resolution" and "flash" architectures, as well as Northrop-Grumman's Σ - Δ configuration.



Fig. 1. Performance regions for RSFQ ADCs with diamonds indicating demonstrated circuits. Filled dot semiconductor data used with permission of Bob Walden and © 1999 HRL Laboratories, LLC. All Rights Reserved.

2.1.1 Phase-modulation/demodulation ADC

Fig. 2 shows a block diagram of a RSFQ "high-resolution" ADC based on a phasemodulation/demodulation architecture (a result of collaboration between HYPRES and SUNY).⁴⁸ The circuit consists of two major parts: a differential-code front-end quantizer and a digital decimation low-pass filter. The front end is composed of analog phase modulator and a digital phase demodulator. The phase modulator consists of a singlejunction SQUID, biased by a DC voltage from a special voltage source, which is stabilized by an internal clock frequency. The phase demodulator consists of a timeinterleaved bank of race arbiters (SYNC) followed by a thermometer-to-binary encoder (DEC).



Fig 2. (left) Block diagram of a phase modulation/demodulation ADC. (right) Chip photo.

The front-end phase quantizer⁴⁹ operates as follows: a DC voltage generator continuously pumps magnetic flux into the superconducting inductive loop of the single-junction SQUID at a stabilized rate of $\frac{1}{2}$ flux quantum per clock period. Inside the loop, this linearly growing flux adds to the signal flux coupled in from the input current. After the total magnetic flux in the superconducting loop reaches a certain threshold, the Josephson junction of the interferometer switches and releases a single quantum of magnetic flux from the loop, (i.e., an SFQ pulse). Thus, for a constant input signal, the junction simply generates a periodic SFQ pulse train at half the clock frequency. When the input signal increases, however, the total flux within the loop grows more quickly, making the frequency of the output pulse train increase. Similarly, when the input signal decreases, the flux within the loop grows more slowly, and, hence, the frequency of the output pulse train decreases. This mechanism, in fact, produces a continuous linear analog phase modulation of the train with 2π of phase corresponding to a single flux quantum worth of input signal coupled into the phase quantizer.⁵⁰

Demodulation of the phase-modulated pulse train is performed using a device called a synchronizer. This synchronizer (sometimes called a "race arbiter") is a specialized RSFQ shift register in which each cell stores the data pulse directed to it, releasing it only when a clock pulse arrives. Several such cells (or "channels") are cascaded in order to eliminate unresolved racing conditions; however, even under racing conditions, the synchronizer never drops pulses, so the DC component of the signal never drifts. A single synchronizer channel provides digitization of the phase to a resolution Least Significant Bit (LSB) value of π , up to an input signal slew rate of ± 1 LSB per clock period. Using a bank of *N* synchronizer channels, uniformly interleaved in time within one clock period, increases this phase resolution to LSB = π/N and limits the input signal slew rate to $\pm N$ LSBs per clock period. In order to obtain a binary differential code from the thermometer

code outputs of the synchronizer bank, the encoder block adds up these outputs and subtracts N/2 each clock period.



Fig. 3 (left) This oscilloscope photograph shows the operation of a 10-bit version of the high-resolution ADC. This chip was operated up to 900 MS/s with a 64:1 decimation filter. (right) Measurement of a 14-bit ADC performance at 175 MS/s (11.2 GHz clock frequency with 1:64 decimation ratio) using an 8K-point FFT spectrum. For 50 MHz input sinewave: ENOB = 8.9 bits, SINAD = 55.3 dB, SFDR = -74.3 dBc (12.3 SFDR bits).

The differential code from the output of the front end is passed to a digital decimation low-pass filter (DSP), which uses a standard CIC (cascaded integrator-comb) architecture [Hogenauer⁵¹] with two integration stages and one differentiation stage. The first integration stage simply restores the signal from differential code, while the second one provides the first-order low-pass filtering.

The dynamic resolution or Effective Number of Bits (ENOB) of this ADC is determined by the input signal bandwidth (BW), the internal clock frequency f_{clk} , and the number of synchronizer channels N and is given by

$$ENOB = \log_2 \left(N f_{clk} / \pi BW \right) + \frac{1}{2} \log_2 \left(f_{clk} / 2BW \right).^{52}$$
(1)

The first term in this formula accounts for the slew rate limit, while the second one comes from standard oversampling gain. Here, the BW is assumed to be half the output sampling rate (i.e. at the Nyquist limit). Therefore, (1) gives a bandwidth-to-resolution tradeoff ratio of 1.5 bits per octave. Output spectra of this ADC for both single tone and two-tone tests is shown in Figs. 3 and 4. Additional details can be found in Refs. 53, 54, and 55.

This ADC design is especially linear, because the quantization thresholds are set by a ratio of fundamental constants (h/2e) in the SQUID in the front-end. This leads to an enhanced spurious-free dynamic range (SFDR) in comparison to semiconductor ADCs, whose thresholds are set by the matching of device characteristics.



Fig. 4 Measured spectra on (left) ADC output for a 10 MHz tone (unfiltered). Note the input tone harmonics; (right) Two-tone ADC test with 8 MHz and 10 MHz signals (filtered). For this initial test, the ADC does not show significant 3^{rd} order intermodulation products.

2.1.2 "Flash" wideband parallel ADC

Fig. 5 shows a circuit diagram and photo of the HYPRES RSFQ *flash* ADC, which is optimized for high bandwidth and clock rate. The flash ADC uses a periodic comparator architecture requiring only N comparators to digitize N-bit data (unlike semiconductor flash schemes which require 2^{N} -1 comparators). In the flash ADC approach, the input signal is delivered to the linear array of N comparators via an R/2R resistive divider ladder, such that each successive comparator in the array receives half of the remaining input signal. This configuration results in a parallel N-bit Gray-code⁵⁶ output at the end of each sample interval.



Fig. 5 (left) Circuit schematic of the RSFQ quantizer of the flash ADC. (right) Flash ADC chip with 2 complete 6-bit flash converters (one in each corner). Each ADC contains 6 pairs of RSFQ quantizers, a start-stop acquisition logic block, and a 6x32 bit FIFO memory buffer.

The flash comparator works as follows: as the input signal increases, more flux is coupled into the quantizer loop. The Meissner effect causes a counteracting circulating

current to be induced, which adds to the current bias flowing through the sampling junction. When interrogated by a clock SFQ pulse, the sampling junction will redirect this flux quantum to the output latch, corresponding to a sampled value of "1". In contrast, as the input signal decreases, less flux is coupled into the quantizer loop, causing less current to add to the sampling junction bias. If a sampling SFQ pulse arrives from the clock in this state, the floating buffer junction connected to the sampling junction will release the pulse; therefore, there will be no signal sent to the output latch. This behavior corresponds to a sample value of "0".

The RSFQ flash comparator design employs a two-spoke SQUID wheel (i.e., a twoleaf phase tree)^{57,58} containing two quantizing junctions. When the phase between these junctions is adjusted to equal π (i.e. ½ flux quantum), the combination acts as if it were a single very small junction. This reduces the effective *LI* product of the comparator circuit, helping to linearize its dynamic performance. A 1-pH shunt inductor in parallel with the input transformer inductance helps to further reduce the *L/R* time constant of the circuit. A small feedback resistor can even be used to further linearize the comparator's dynamics at high frequencies. Fig. 6 shows "beat frequency" signal reconstructions from a 5-bit raw Gray-code RSFQ flash ADC. The onset of dynamic distortion can be seen as the input frequency increases. The bandwidth of this front end has been demonstrated in beat-frequency tests up to 30 GHz.



Fig. 6 A panel of oscillographs showing the performance of the flash ADC plotted in Fig. 1, (from left to right) 5 bits at 4 GHz, 4 bits at 12 GHz and 3 bits at 20 GHz.

The 1-cm² digitizer chip (shown in Fig. 5) contains two 6-bit transient digitizers. This circuit is a six-bit version of the ADC used in the beat-frequency tests; however, for each bit, an acquisition switch set and a 32-stage acquisition shift register were attached to the comparator's clock and data output ports. Using this design, single-shot pulses with risetimes < 100 ps were digitized (see Fig. 7). Here, the sampled data reveals structures that suggest ringing which is not visible on the sampling scope reference. The bandwidth of this ADC test chip has been shown to exceed 10 GHz (the 3 dB point is at ~16 GHz).

When comparator threshold distortions are present, there is a marked decrease in ADC resolution. Architectural improvements, including redundant comparators and realtime digital error-correction logic, can restore much of this lost performance. By interleaving several identical comparator thresholds, using XOR logic to combine pairs of thresholds, then XOR-ing those thresholds, new thresholds for additional bits of resolution can be synthesized.⁵⁹ In addition, the MSB comparators receive the smallest fraction of signal current, resulting in the widest "gray zone" near the threshold. By interleaving the thresholds of two comparators per bit, and using real-time RSFQ digital logic, the comparator furthest away from its gray zone can be chosen. The algorithm uses the output from the previous bit to choose the correct comparator, hence the name "lookback" logic.⁶⁰ Fig. 8(left) shows a prototype Flash ADC chip with these additional features.



Fig. 7 Reconstructed sampled data from an RSFQ Flash ADC digitizer. (left) A periodic analog pulse signal captured on a sampling oscilloscope; (middle) 8 GS/s single-shot data; (right) 16 GS/s single-shot data.



Fig. 8 (left) The advanced Flash ADC architecture with interleaving and lookback logic. (right) A "ping-pong" time-interleaved configuration for a 40 GS/s bunch profiler.

Very high frequency semiconductor ADCs often use a "ping-pong" architecture, in which two separate ADCs work in tandem, sampling the input signal 180° out of phase in order to effectively double the sampling frequency. This approach also works with

RSFQ ADCs. Fig. 8(right) shows a set of twin Flash ADCs arranged to form a 40 GS/s "bunch profiler" for application in high-energy physics experiments for the US Department of Energy. Although quite different at the device level, this design demonstrates the ability of RSFQ circuits to re-use existing architectures from traditional IC design. The flash ADC could also be used as a front-end component for a number of envisioned applications, including transient digitizers, channelized wideband receivers, and digital beamforming receivers.

2.1.3 Sigma-Delta ADC

Semiconductor ADCs have used an architecture known as a Σ - Δ modulator for some time.⁶¹ Several groups are investigating whether or not RSFQ technology can also be used to implement this type of ADC. The traditional Σ - Δ approach uses an op-amp to add up successive digital samples (the Σ operation) and then subtract the generated digital word from the total input signal (the Δ operation). The modulated digital signal is sent to an integrator (low-pass digital filter) where the Nyquist-rate digital words are generated. Fig. 9 shows the circuit photo and schematic of a single flux quantum Σ - Δ modulator design from Northrop-Grumman (Baltimore, MD).^{62,63,64} The modulator uses a superconductive inductor at the input to integrate the applied signal voltage and then a single junction quantizer to digitize the integrated current. The Δ -feedback is in the form of SFQ pulses. An advantage of using SFQ pulses as this feedback is that each pulse is identically repeatable and accurate. However, the striking disadvantage is that the bulk of signal processing to make an ADC must take place in conventional electronics.



Fig. 9 (left) Σ - Δ modulator circuit photo. (right) Σ - Δ modulator circuit diagram. (Photo courtesy J. Przybysz, Northrop-Grumman.)

The circuit is clocked by sampling pulses generated by a 1.28 GHz room-temperature source and sharpened by a pulse buffer before being applied to the modulator. Each time the sum of the sampling pulse current, the junction bias, and Σ -inductor current exceed the critical current of the sampling junction, the quantizer produces an SFQ Δ -feedback pulse and reduces the current in the inductor by Φ_0/L . The Fourier transform of the output of a second-order modulator after processing shows outputs (Fig. 10) with a reduction in quantization noise at low frequencies near the signal frequency.



Fig. 10 Northrop Grumman second-order Δ - Σ modulator data FFT showing second-order noise shaping. (Photo courtesy J. Przybysz)⁶⁵

2.2 Digital-to-analog converters

A number of different programmable Josephson voltage standards have been proposed.^{66,67} All of these designs are essentially digital-to-analog converters (DACs) based on the properties of flux quantization. The fact that an SFQ DAC uses the same fundamental physics that define the unit of the Volt has some profound consequences. For instance, any instantaneous voltage generated by the DAC will be precise to the accuracy of the definition of the Volt. Further, every waveform cycle generated will be *exactly* the same, with quantum precision. The intrinsically small time constants associated with Josephson junctions may make it possible to extend such performance to many GHz, although very large arrays of JJs may be necessary to achieve useful levels of output voltages.

2.2.1 Voltage-multiplier Josephson DAC

Vasili Semenov at SUNY Stony Brook first suggested an RSFQ DAC design based around a voltage multiplier (VM) block.⁶⁸ This DAC (seen in Fig. 11) uses each bit of an *N*-bit RSFQ digital word to drive an RSFQ digital-to-frequency converter (DFC) (sometimes noted as "SD"). A DFC is designed to output a stream of SFQ pulses at a frequency that is proportional to its reference clock frequency, only when the bit value at its input is "1". By arranging a series of *N* DFCs with reference frequencies f_N that decrease as 2^{-N}, one can effectively create a binary-weighted set. By switching different DFCs in and out of the series with the digital input word, any of 2^N combinations can be chosen. The VM is an inductively-coupled SQUID chain used to transform the DFC streams of flux quanta into time-averaged voltages, then sum them, creating a corresponding output voltage with *N*-bit resolution. This arrangement constitutes a programmable Voltage Standard, since the output voltage is derived directly from the input word and the Josephson frequency-to-voltage relation. By updating the *N*-bit input word periodically, at a rate slower than the slowest DFC reference frequency, one creates a DAC. The voltage at the output of the DAC during a single sampling period is given by $V_{out}=M\Phi_0f_0$, where f_0 is a readout or sampling clock frequency, and *M* is the total number of SFQ pulses driven through the VM by all the DFCs. The LSB of the output voltage is $n \cdot \Phi_0 \cdot f_0$, where *n* is the number of stages in the smallest stage of the VM, and f_0 is again the output sample rate. The output dynamic range is 2^N ·LSB, where *N* is the resolution of the DAC in bits.



Fig. 11. (left) DAC chip. (right) DAC block diagram. (Figures courtesy of V. Semenov, SUNY Stony Brook.)

Fig. 11 shows a chip photo and block diagram of the voltage multiplier DAC. Many bits of dynamic range are possible, because the initial reference clock can be very high. For instance, the chip in Fig. 11 is a 22-bit DAC. Experimental results of an 8-bit design are shown in Fig. 12. The differential non-linearity of the DAC is excellent (< 0.1 LSB). With the proper microwave engineering of the VMs, a multi-GHz output rate (effective bandwidth) could be achieved, while maintaining significant dynamic range. The update clock and output clock are synchronized to prevent spikes during code transitions.



Fig. 12 (left) Deviation of measured quantization levels from the expected uniform positions. (right) Dependence of output voltage of the DAC on applied digital code. (Figures courtesy of V. Semenov, SUNY Stony Brook.)

2.2.2 Pulse-driven Josephson DAC

The National Institute of Standards and Technology (NIST), (Boulder, CO) has also been developing a Josephson DAC which exploits single flux quantum pulses to create a programmable or "AC" voltage standard.⁶⁹ It is shown in Fig. 13. To operate, a desired tone (or any other periodic waveform) is first synthesized. A Σ - Δ modulator algorithm is implemented in a computer program to generate a set of digital samples of this given periodic waveform S(t), which is stored in the memory of a semiconductor digital code generator. This data, S(i), is used to generate an output digital pulse code, $S_D(t)$, in which the density of ones is proportional to the magnitude of the original given signal. Naturally, the sequence will S(i) contain harmonics of the desired waveform (i.e. quantization noise) which is characteristic of the sampling process. By using a Δ - Σ modulation approach, however, this quantization noise can be substantially reduced or "pushed out-of-band". If the digital code generator were ideal, S_D could simply be low-pass filtered and used as the analog waveform; however, real digital code generators have both amplitude and phase distortion – this is where using flux quantization helps.

It has been shown that the Josephson frequency-to-voltage relation holds for pulsedriven Josephson systems, just as for sinewave-driven systems, as long as the frequency of these pulses is below the junction plasma frequency.⁷⁰ In this case, S_D is applied to a JJ array at a few GHz. The instantaneous oscillation frequency across the array is then simply proportional to the time-averaged voltage or density of ones (i.e. density of digital code generator pulses) being driven across it. The JJ array serves to quantize the time integral of these voltage pulses by Φ_0 , which cleans up many of the non-idealities in S_D . The resulting output S_J can then be applied to an analog low-pass filter to recover a much higher fidelity output signal S'(t). Fig. 13 (right) shows the output spectrum of this DAC generating a 23.4 kHz sinewave. The second harmonic is clearly suppressed to about -75 dBc. In the absence of noise or jitter, this should increase to <-100 dBc. The output voltage swing of the generated waveform is proportional to the number of junctions in the array. A 1000-junction array could generate waveforms a few milivolts peak-to-peak, so much larger single-chip arrays would presumably be needed for most applications.



Fig. 13 (left) Block diagram and (right) measurement results of pulse-driven Josephson DAC being developed at NIST for AC voltage standards. (Figures courtesy of S. Benz, NIST)⁷¹

3. RSFQ DSP and Infrastructure Blocks

Basic digital processing functions are performed in RSFQ as in any other logic family. For carrying out the manipulation of bits, adders, multipliers, clocks, registers, interconnects, and data buffers are all needed, with active Josephson transmission lines (JTLs) to serve as delays for time synchronization⁷². Other blocks include parallel-toserial converters, clock generators, and phase-locking devices. The diversity of components that have been (or are being) developed has brought RSFQ technology to the point where the design of larger systems with more functionality can be reasonably considered. Several key blocks for general DSP applications are covered in this section. The discussion of the applications themselves is reserved for section 5.1.

3.1 Digital clocks and phase-locked loops

The naturally high frequency of RSFQ circuits requires that digital clocks of equally high frequency be generated and distributed throughout the chips themselves. For "low-speed" circuits (i.e. ≤ 20 GHz) it is often convenient to use an external synthesized source to create a sinewave clock trigger that can be sent to the chip via high-speed coaxial cable; however, when useful systems are considered, a more practical method of clock generation is required. Further, the necessity of having very fast RSFQ circuits operate with the traditional semiconductor-based instrumentation leads to a requirement not only for an on-chip RSFQ clock, but also for it to be imbedded in a full phase-locked loop (PLL) to create a complete useful RSFQ subsystem. The effective implementation of RSFQ clock controllers (a key component to enabling large-scale RSFQ systems) was pioneered by Lin and Semenov (see Ref. 73).

3.1.1 On-chip clock sources

The characteristics of several SFQ clock sources are summarized in Table 1. These include single over-biased junctions (which do not have particularly narrow linewidths due to thermal noise), JJ arrays (which require special care in ensure coherent radiation), JTL oscillator rings (which are easy to design, but offer only limited tuneability)⁷⁴, and so-called "long" Josephson junctions (which can be operated in either flux-flow or resonant modes).

Oscillator Type	Quality Factor	Frequency
Single Junction	$10^2 - 10^3$	>100 GHz
Junction array	$10^3 - 10^5$	>100 GHz
Long junction (flux flow mode)	10 ³	>100 GHz
JTL oscillator ring	$10^3 - 5 \ge 10^3$	$10-20 \; GHz$
Long Junction (resonant mode)	$10^{5} - 10^{6}$	1 – 100 GHz

Table 1. A comparison of different single flux quantum clock sources

High quality room-temperature clock sources at these high frequencies, which could be used to externally clock the circuits, are extremely expensive, difficult to package, and suffer strongly increased timing jitter when transmitted over long distances. Increased jitter would prove detrimental to the performance of any digital circuit. For these highspeed integrated circuits, a low-jitter, on-chip clock technology is needed. An on-chip clock technology consists of four key building blocks: a stable, low-jitter master clock generator; a clock distribution network; a clock decimator and selector to generate and select a sub-harmonic of the master clock frequency; a phase-locked loop (PLL) to synchronize the on-chip master clock with a stable external clock to provide long term phase stability.



Fig. 14 Measurements of a 56.6 GHz LJJ resonator SFQ clock pulse train digitally divided by 2^9 for display in (left) Time-domain showing a period 256(T) = 4.52 ns and (right) Frequency-domain with f/256 = 221 MHz.

An example of a high-quality on-chip SFQ clock is shown in Fig. 14. The long Josephson junction (LJJ) oscillator in resonant mode offers a compromise between tunability and stability. By biasing on the N^{th} zero-field step (ZFS) of an LJJ (N = 7 in Fig. 14), a train of SFQ clock pulses can be generated at the resonant frequency set by the LJJ's size, or alternatively, at any higher harmonic of this characteristic frequency.⁷⁵ Digital frequency dividers can also be used to access sub-harmonics of the clock pulse train.

Other approaches have also been employed to generate a SFQ clock on chip, while maintaining synchronization with room temperature electronics. One approach employed an SFQ clock coupled to a resonant length of microstrip transmission line, so that the clock becomes "locked" at the resonant frequencies of the microstrip line.⁷⁶ Another variation employed a frequency doubling technique in which two SFQ pulses are produced for every one that is input, so that several cascaded doublers can bring the frequency up to the range of interest.⁷⁷ The first of these is a narrow-band approach, suitable for specific frequencies, when tuning is not needed. The second is somewhat limited in range and lacks a feedback mechanism for long-term stabilization.

3.1.2 Phase-locked loops

A more traditional approach to synchronization – the PLL – is shown in Fig. 15.⁷⁸ The layout on the right is an RSFQ PLL suitable for use with any standard RSFQ circuit. The basic phase-locked loop design is that of a classical digital PLL,⁷⁹ in which the phase detector and the frequency divider are digital, but the loop filter and voltage-controlled oscillator are analog. Here, the VCO is an over-biased Josephson junction and the clock output is a train of SFQ pulses. Although certainly not the highest Q resonator, it is nevertheless a suitable (and simple) method for this proof-of-principle design.

In this circuit, the fast output of the VCO is phase locked to a slower reference generated at room temperature signal by first passing through a frequency divider (a toggle flip-flop counter) and then being compared against the reference signal in the phase detector. The phase detector is a device that compares the phases of the two SFQ pulse trains at its inputs and issues an analog feedback signal proportional to the difference in phase between the signals. This output signal is the filtered by a loop filter (it may also be amplified or attenuated as necessary) and fed back to the VCO bias in order to minimize the phase difference between the two signals. Fig. 15 (right) shows an on-chip phase-locked loop (PLL) operating at 50 GHz and locking to a reference frequency over a range of 1.5 GHz (\pm 1.5%). The pull-in and locking ranges were indistinguishable.



Fig. 15. (left) Layout of an RSFQ PLL (right) PLL demonstration at 50 GHz VCO frequency. Traces show phase matching at 12.2 MHz between reference clock and frequency divider output, and phase detector output. The two signals are out of phase by 90 degrees.

3.2 RAM and FIFO buffers

3.2.1 Random access memory

Because it is composed of a ratio of fundamental constants, the magnetic flux quantum (Φ_0) , stored as a persistent current in a superconductor, is an excellent choice for a unit of data storage for large memories. The ability of such flux quanta to be both stored and transferred with virtually no power dissipation allows the development of various large-

scale circuits with on-chip memory, connecting them into deeply pipelined devices. While RSFQ logic designs successfully use these features, RAM designs have historically not fully exploited this ability.

The most successful superconductor RAM implementation thus far is one from NEC.⁸⁰ The design approach used in the NEC memories combine SFQ memory cells with AC-powered voltage-state Josephson periphery circuits (readout, decoder, etc.). Unfortunately, the requirement of large external AC-power limits the clock cycle to about 1 GHz, making the RAM throughput insufficient to match the much faster, DC-powered, RSFQ logic family.⁸¹ Recently, however, new DC-powered SFQ RAM approaches have been pursued that may help this issue.^{82,83}

One new DC-powered Cryogenic RAM or "CRAM"¹²⁹ consists of SFQ memory cell arrays, dc/SFQ decoders, current drivers, sensing gates, and block multiplexor and demultiplexors. The general structure of the RAM is shown in Fig. 16. In order to increase throughput, a 16-Kbit RAM chip is divided into four 4-Kbit blocks. Each block comprises a row-accessible 128 x 32-bit matrix, where each row of contains one 32-bit word. A block demultiplexor distributes input data between blocks, where a decoder converts address and/or data into DC currents on microstrip lines, which propagate near the speed of light, to operate on rows of SFQ memory cells. In a READ operation, a 32-bit RSFQ word appears across the block output and is funneled to the CRAM output by a block multiplexor.



Fig. 16. (left) Block diagram of the CRAM combining four blocks of memory arrays, a block decoder, Y-decoders, select line drivers, sense gates, and output block multiplexor; (right) Single block of the CRAM including an address decoder and drivers, a 32x128 memory cell array, X-drivers, and output sense dc-to-SFQ converter.

Fig. 16 (right) shows a more detailed schematic of a single 4-Kbit memory block. Access to individual SFQ memory cells is provided via both magnetically coupled and direct microstrip lines. The sign of the currents depends on whether READ or WRITE operations are selected. Each WRITE1 operation is preceded by an erase or WRITE0 to reset the cell. The SFQ memory cell itself (see Fig. 17) is based on a modified version of the NEC vortex transition (VT) memory cell^{84,85}, with non-destructive readout and current control. If the read-out SQUID switches to the resistive state during a READ operation, the Y-column sense read-out cell (dc-SFQ) transforms the DC-signal into an RSFQ bit.



Fig. 17. An SFQ memory cell with DC-powered row-accessible selection.

3.2.2 FIFO memory buffers

First-In First-Out (FIFO) memory buffers (of the type used in section 2.1.2) can be created using basic shift register cells. The first RSFQ shift register was a simple chain of RS flip-flops successively clocked by an SFQ pulse on a Josephson transmission line (JTL) traveling opposite to the data stream. This simple design later extended, with an additional clock JTL, to build a *reversible* shift register.⁸⁶ The subsequent merging of the clock JTL and data RS flip-flop into a single cell resulted in a junction-efficient shift register design with only two junctions per bit, often called a "2-JJ" design shown in Fig. 18.⁸⁷ All these designs have a constraint between the delay of the clock pulse τ_{clk} and the delay of the data shift τ_{shift} to avoid racing conditions. Specifically, the clock delay τ_{clk} must be negative (i.e. the clock and data must travel in opposite directions), and must be greater than τ_{shift} : (- τ_{clk} > τ_{shift}).⁸⁸

Fig. 19 shows the measurements of 256×1 -bit and 4×1 -bit 2-JJ shift registers at 12.36 Gb/s and 60 Gb/s, respectively.⁸⁹ In Fig. 19(left) the envelope of a directly triggered measurement of the shifted sequence (1110011) at 6.18 GHz is shown in trace (a). Increasing the dc/SFQ clock trigger offset, the input clock frequency can be doubled. The consequence is seen in (b) where the output envelope is moved to a new position in time (by half the delay of the shift register). Specifically, $\frac{1}{2} \cdot (6.18 \text{ GHz})^{-1} \cdot (256 \text{ bits}) = 20.7 \text{ ns}$, corresponding to an operation at the double frequency 12.36 GHz. Trace (c) corresponds

a leap to the position when the dc/SFQ converter generates the clock pulse train. Similar measurements of a 2-JJ 32-bit shift register yielded proper operation at a 31.8 GHz clock frequency.



Fig. 18 The most common "2-JJ" RSFQ shift register design, which features reversible operation as well as a minimum number of junctions per cell. Clock distribution junctions are on the top of the circuit, while data storage registers lie across the bottom.



Fig. 19 Shift register measurements. (left) Triggered clock test of a 256-bit SR with a data pattern of (11100111) at 885 MHz for clock frequencies of: (a) 6.18 GHz (b) 12.36 GHz and (c) >2.4 mA (clock pulse train generation). (right) Non-triggered clock test of a 4-bit SR showing correct operation to ~124 μ V (~60 GHz). Vertical scale 9.7 GHz/div. (frequency = <voltage>/(*h*/2*e*)). Horiz. scale 50 μ A/div.

In an un-triggered high-frequency test, a ~1-200 Hz triangle wave (sweep) current is applied to the input of a dc/SFQ converter (the generator of the clock pulse train), and the time-averaged DC voltages on both the clock JTL and the output of the shift register are measured, with the data signal frequency adjusted in order to observe a few data envelopes in each sweep period. Fig. 19 (right) shows the high frequency un-triggered measurement of a 4-bit buffered shift register using this method. When operating correctly, the digital SR output voltage is the same as the voltage on the clock JTL whenever the data value is a "1". The digital SR output voltage is zero when the data value is "0". In this measurement, beyond ~124 μ V (or ~60 GHz according the Josephson

voltage-to-frequency relation), the output no longer follows the clock. This sets the maximum operational frequency. Even these speeds are still lower than the simulated maximum frequency 75 GHz. This is due to: the maximum frequency of the input dc/SFQ converter (~65 GHz); underbiasing of the shift register due to the small parameter margins of some cells; and the resonances in the DC bias lines.

3.3 Adders and multipliers

In general, the throughput of a computational process can be increased at the expense of latency by using a pipelined architecture. Such pipelining normally requires additional registers, which in a semiconductor technology can more than double the size of the circuit. In RSFQ logic, however, register storage is built into the gate itself. This inherent memory state (i.e., storage of single flux quanta) makes it possible to build a basic set of useful cells from Toggle and Reset-Set (T and RS) flip-flops and their modifications. Such modifications can include adding destructive and non-destructive readouts (DROs and NDROs), as well as fan-in buffers (often called "confluence buffers" or "mergers"), and fan-out cells (typically called "splitters"). Using this technique, basic cells have been developed to execute many common digital signal processing (DSP) elementary operations, including Addition, Accumulation, and Multiplication. Details of the design and experimental evaluation of such cells have been extensively described in the literature¹⁰, therefore only a few examples will be given here. An excellent self-contained full "design example", can also be found in Ref. 90; providing a detailed discussion of the cell timing and clock distribution, simulation and verification, and even yield and bit error-rate estimation for an RSFQ pipelined parallel adder design.

3.3.1 Basic DSP gates

Since all these cells have an internal memory, they provide their own registers to synchronize and effectively pipeline their inputs and/or outputs. For a basic latching data register, an RS flip-flop or destructive read-out (DRO) call as in Fig. 20 can be used. Combining a T flip-flop with a DRO and confluence buffer performs the function of half or full addition (FA-cell).⁹¹ As another example, a D flip-flop with non-destructive read-out (NDRO or NR-cell) and confluence buffer can be used to realize the function of accumulation as shown in Fig. 21.^{92,93}



Fig. 20 (left) Circuit and (right) block diagrams for a D flip-flop used as a destructive readout cell.

To take advantage of the speed (and hence throughput) of RSFQ, serial math approaches have been explored. For implementation of serial addition, an entire carry-save serial adder (CSSA-cell), as seen in Fig. 22, has even been designed. This cell is an excellent demonstration the capabilities of a "non-Boolean" design approach to RSFQ.⁹⁴



Fig. 21 (left) Circuit and (right) logical diagrams for a non-destructive read-out cell.



Cany-Save Serial Adder (CSSA)

Fig. 22 (right) Circuit and (right) logical diagrams for the CSSA.

The implementation of these gates is detailed in section 3.3.3. Another set of basic RSFQ cells has also been successfully developed and reported on.⁹⁵ Furthermore, a traditional approach of composing DSP elementary functions using RSFQ Boolean cells and flip-flops has been described as well.⁹⁶

3.3.2. The B-flip flop

Success in the design and demonstration of RSFQ functional blocks, such as those in section 3.3.1, was accompanied by development of a "universal" RSFQ cell. The idea of the "bi" flip-flop or B-flip flop (shown in Fig. 23) was to take advantage of the inherent memory capability of RSFQ logic to form a template cell, from which a number of useful functions could be derived simply by connecting different cell inputs and/or outputs, with shorting or opening of different branches.⁹⁷ The B flip-flop has 4 inputs and 6 outputs

altogether. Input SFQ pulses can change the internal state ("1" or "0") of the cell by introducing a flux quantum into the center, shared interferometer. This internal state, along with additional input pulses, can then define logical outputs with reference to different points in the cell. Major modes include RS^2 , T^2 and $T \cdot RS$ configurations,⁹⁸ which utilize an input toggle of the memory state, a persistent set-until-reset state, or a combination of both. Possible logical operations include NDRO-cell, toggle flip-flop with synchronous destructive readout (T1-cell), full-adder, or even an asynchronous (reversible) up-down counter. This template also serves as the basis for the gates described in section 4.1.



Fig 23. An approach to a template RSFQ gate, the bi (B) flip-flop, here configured in RS^2 mode. Logical expressions at the outputs indicate the dependence on the inputs.

3.3.3 Serial vs. parallel architectures

As previously mentioned, the high speed and naturally pipelined architecture of RSFQ logic makes it possible to consider both parallel and serial approaches to computeintensive functions. Specifically, multi-rate processing, in the form of serial math, is one method to take advantage of the very high clock speeds available, while minimizing the total number of devices needed for a given task.

The most common DSP functional primitive is X = WY + Z. In order to perform this function, both multipliers and adders are required. Fig. 24 shows single-bit modules for both serial and parallel implementations of multipliers. These modules can be designed using the basic set of RSFQ cells described above; then interconnected with JTLs to provide SFQ pulse transmission and to set the necessary delays within and among them. For example, a serial multiplier module which dissipates only 13 μ W has been constructed using 48 Josephson junctions (JJs).⁹⁹ The parallel multiplier module (PMM), also shown in Fig. 24, employs a total of 67 JJs and dissipates only 19 μ W of power experimentally at 15 GHz.¹⁰⁰



Fig. 24 Block diagrams of (left) an RSFQ serial multiplier and (right) single bit slice of an RSFQ parallel multiplier.

The serial-multiplier in Fig. 24 uses three elementary RSFQ DSP cells: destructive readout registers (DROs or DRs), NDROs or NR cells, and carry save serial-adders (CSSAs). After clearing the internal carry bits of the CSSA, N-bit operand B is loaded (either serially or in parallel) into the top N-bit DROs where it will be held for the multiplication cycle. If successive multiplies by the same coefficient value are required, operand B need only be loaded once. An N-bit operand A is then shifted into the DR register from the right, LSB first. After the first clock, the LSB of the result product is available at the sum output of the rightmost CSSA. Operand A is shifted N times and then padded with zeros and shifted N more times to produce a 2N-bit product shift out to the right from the rightmost CSSA. At the end of each clock period, the serial-multiplier delivers each consecutive bit of the 2N-bit product $(A \times B)$ at the output terminal. The partial single-bit multiplications are performed by the AND cells, while the CSSAs sum up the partial products. The whole multiplication takes 2N clock periods; however, loading of the next B operand can take place during the last N periods of the previous multiplication cycle. This is a highly efficient method of multiplication and forms the basis of the FFT processor described in section 5.1.7.

Built-in self-test (BIST) circuitry is necessary to perform the GHz rate digital testing necessary for this cell. The placement of FIFO memory buffers at the input and output of the cell under test (CUT) provides a method of loading in a test vector at low-frequency, then switching to a high-speed signal, which clocks the CUT and stores the output in another on-chip buffer, where it is again available for low-frequency readout. Such high-speed tests are shown in Fig. 25.¹⁰¹



Fig. 25. (left) High-speed operation of an 8-bit serial multiplier with shift register test system at 6.3 GHz and 33 MHz load/off-load clock. Inputs: $W=\{11111111\}$, $Y=\{11000000\}$; output $YW=\{1011111101000000\}$; (right) Correct operation (WX + Y + Z) of a parallel multiplier module with shift-register test system at 5.3 GHz (load/off-load clock is 2.5 MHz) for W=X=(0000101), Y=(0110101), and Z=(1010001). The outputs for both are in NRZ format.

A consequence of the high speed of RSFQ logic is that additions and multiplications can be implemented as either parallel or serial operations, without much reduction in performance. If both operations are bit-wise pipelined (i.e. no carry propagation) then circuit complexity can be directly traded for execution time. For example, as previously mentioned, an *N*-bit \times *M*-bit multiplication requires $N \times M$ addition operations; however, these can be accomplished as either *M* additions over *N* clock cycles, or by $N \times M$ additions in only one clock cycle. The parallel implementation of a 16-bit multiplyaccumulator requires 288 full adders; however, a serial implementation requires only 33 Carry Save Adders (CSA). With an internal clock rate of 32 GHz, it would perform the operations at a throughput of 1 GHz. An intermediate trade-off could also be designed, such as using 64 adders over 4 clock periods. This tradeoff example give a good feel for the design flexibility enabled by the high-speed bit rates possible in RSFQ.

4. RSFQ Chip I/O Approaches

An extra level of complexity exists at the interface between RSFQ circuits and offthe-shelf components. This is due to the high aggregate data rates involved, the cryogenic nature of the technology, and the low-level signals of RSFQ. One method for bringing data onto or taking data off an RSFQ chip is to perform time-division multiplexing / demultiplexing. Such "muxing / demuxing" of data can be done synchronously or asynchronously, depending on whether clock recovery is required between data source and destination. The low-level superconductor digital signals can be somewhat amplified to a point where custom semiconductor digital amplifiers can provide output at standard emitter-coupled logic (ECL) levels. Further, direct high-speed data I/O may be possible using on-chip electro-optic techniques. In many cases, partitioning of an RSFQ system may involve the use of a superconductor multi-chip module, which can allow direct data transmission between chips at tens of Gb/s. Ultimately, it is the cryopackage containing the RSFQ chip or MCM that actually interfaces with the cooling apparatus and I/O path which sets the final cooling requirement.¹⁰²

4.1 Multiplexors and demultiplexors

The B flip-flop with joined inputs (or T^2 flip-flop), as described in section 3.3.2, can be used as an RSFQ dual-rail (asynchronous) demultiplexor. The circuit in Fig. 26 (left) has two input lines – one for input zeros "In 0" and one for input ones "In 1". The ones are applied to the input of one internal T flip-flop and the zeros are applied to the input of the other internal T flip-flop. In this configuration, the direct and inverted outputs of each T flip-flop form the dual-rail (asynchronous) demultiplexed output "Out A and B".



Fig. 26 (left) The schematic of a T^2 -mode B flip-flop configured as a dual-rail 1:2 demultiplexor and; (right) schematic of an asynchronous multiplexor cell of similar design.



Fig. 27 (left) Functional test of the T^2 demultiplexor cell showing correct operation. All outputs are NRZ data. (right) High-speed test results of the T^2 demultiplexor cell. (Horiz. axis units – mA; Vert. axis units – mV.) One trace is the time-averaged voltage input to "In 0". The other is a trace of twice the time-averaged voltage on "OutA 0". Correct operation is seen to the point where the two traces diverge. Input test pattern is (00011011) which is correctly shuffled between OutA and OutB up to 95 Gb/s.

In order to determine the maximum working speed of this demultiplexor, a timeaveraged DC I-V characteristic is measured. Scanning a current on the input "In 0", the dc voltage response on the "In 0" and "OutA 0" terminals can be monitored. Fig. 27 (right) shows the I-V curve from this experiment. For convenience, the voltage on "OutA 0" terminal was multiplied by two. As seen, the traces coincide up to 1.9 mV, which means the maximum working frequency is 95 Gb/s, according to the Josephson frequency-to-voltage relation. Of course, this is not a complete test for such circuit, but it does give a good estimation of the limit of performance the demultiplexor.

A schematic of an asynchronous dual-rail 2:1 multiplexor is shown in Fig. 26 (right). This cell is also based on the B flip-flop, with output terminals serving as inputs and vice versa. The input inductances serve as buffers for incoming data. In the initial state, junctions J1 and J8 are not biased, causing data arriving to input B to be stored in the L2 or L4 buffer and to wait for data arrival on input A. Meanwhile, junctions J4 and J12 are biased, which allows data (either "0" or "1") arriving to the input A to pass through the inductor L3 (or L5). The multiplexor internal state toggles with a delay provided by shunt resistor R, allowing the data captured in input buffers to be released. The multiplexor alternates between the two incoming data streams, doubling the output data rate. If desired, these multiplexor cells can be connected to a tree comprising a 2^{N} :1 multiplexor with no data transfer rate reduction. This scheme also enables parallel-to-serial conversion of dual-rail data at an extremely high frequencies. Simulations predict good operation up to data rates of 60 Gb/s.



Fig. 28 1:8 RSFQ demux operating at 20 Gb/s.

For synchronous operation, another shift-and-dump (serial-to-parallel converter) architecture can be use for demultiplexing. Fig. 28 shows a fabricated 1:8 demux circuit of this type. For eight clock cycles, a serial bit is loaded into the demux cell; the ninth clock dumps these bits onto eight separate output lines, clears the internal demux registers, and begins a repeat of the process. The 8:1 decimated clock is also made available at the output in order to synchronize the data flow between cryogenic and room temperature circuits. Fig. 28 (right) shows a BIST test (as described in section 3.3.3) for a serial data stream (bottom trace) that is sent to the demux cell at 20 Gb/s and correctly shuffled between eight parallel output lines (topmost traces), reducing the aggregate data rate to 2.5 Gb/s per channel.

4.2 Digital output drivers

For electrical connection outside RSFQ chips, the digital data, in the form of SFQ pulses, must be translated into voltage swings suitable for processing by standard semiconductor circuits. The SFQ/dc converter cell¹⁰ is one way of starting this process; however, this method only provides a ~250 μ V NRZ voltage swing for each true bit at the chip pad. So-called "high-voltage driver" (HVD) blocks (similar to the type shown in Fig. 30) have therefore been developed to convert RSFQ data/clock signals into ~2.5 mV NRZ voltage swings at the chip pad.^{103,104,105}



Fig. 29. (left) Output of 2.5 kA/cm² asynchronous voltage driver circuit for 1 Gb/s, 4 Gb/s and 8 Gb/s input patterns and (right) output eye diagram of (a) 1 kA/cm² and (b) 2.5 kA/cm² driver circuits for 4 Gb/s PRBS input. (Photos courtesy of Conductus, Inc.)

A HVD output driver fabricated with critical current densities of $J_c = 2.5$ kA/cm² can operate well up to 8 Gb/s, with rise and fall times of about 100 ps. The outputs of the high-voltage driver circuit for input pulse patterns at 1 Gb/s, 4 Gb/s and 8 Gb/s are shown in Fig. 29. Note that the 2.2 mV output amplitude at 8 Gb/s is less than the 3 mV amplitude measured at 1 Gb/s. A large part of the decreased output amplitude at higher frequencies is due to increasing loss in the measurement probe. The output eye diagrams for a 4 Gb/s pseudo-random binary sequence (PRBS) pattern input are also shown in Fig. 29. Here, the performance of the circuit is gauged by the size of the eye opening, which improves with larger SNR, smaller phase noise, and smaller rise and fall times. The eye opening represents the region, in voltage and time, of error-free operation. Clearly, the 2.5 kA/cm² circuit has a larger eye opening, primarily due to faster rise and fall times, which are about 50% of those for the 1 kA/cm² circuit.



Fig. 30 Mask layout of an RSFQ High voltage Driver (HVD) for amplifying NRZ output voltage swings for measurement off-chip. SFQ pulses are amplified by the input JTL on the right and used to trigger a voltage across the SQUID stack in the center for output across the resistor at the left.

4.3 Electrical and optical signal conversion

Although RSFQ circuits are capable of internal operation at tens of GHz their application is limited by the output drive capability. For data communication applications that require high-speed outputs such as switches and transmitters, the usable bandwidth of an RSFQ circuit is limited by the output interface. The RSFQ signal must be amplified on chip at low temperature to a large enough level to be sensed by a low-noise, wideband, semiconductor amplifiers with a low error rate. Once amplified, the signal can be used, for example, to drive a laser diode or optical modulator for fiber-optic communication links. Approaches under investigation are introduced in the following sections.

4.3.1 Conversion between RSFQ and Emitter-coupled logic (ECL) signals

In order to be compatible with standard off-the-shelf data acquisition systems, most RSFQ output interfaces rely on conversion to ECL representation of ones and zeros.^{106,107} Fig. 31 (left) shows SFQ-to-ECL interface boards capable of handing up to 16 channels of superconductor data at rates up to 1 GS/s. (see Fig. 32)



Fig. 31 (left) ECL interface in a VME cage consists of one clock board and four 4-channel data receiver boards; (right) On-site interface of a RSFQ ADC and a semiconductor DRFM in a VME cage.

The design consists of amplifiers, followed by a discriminator circuit and level shifters (DC restore) to provide standard ECL data waveforms. Whereas previous boards utilized differential outputs, the 1 GS/s modules operate with single-ended clock and data signals

from the chip. Boards have been fabricated / operated in both VME and VXI standards to allow compatibility with various existing high-performance electronics systems such as the DRFM in Fig. 31 (right).



Fig. 32 Output-board amplifier test showing a pseudo-random bit sequence of 3 mV data at 1 Gb/s to simulate the output signals from an RSFQ chip (left) and the eye-diagram of the 1 V amplified digital stream ready for interface to room-temperature electronics (right).

4.3.2 Conversion between optical signals and RSFQ

Interfacing to low-temperature RSFQ devices presents a number of challenges, because the traditional method of connecting to high-frequency (multi-GHz) devices (co-axial cables) introduces a significant heat load into the system. The large physical size of such cables may also limit the total number that may be fit into a given location. If the co-axial cable is more than a few meters long, substantial attenuation due to skin effect losses at higher frequencies may become a problem as well. In comparison, optical fibers have low thermal conductivity, are immune to electromagnetic interference (EMI), are physically smaller and lighter than standard cable, and are not subject to cross talk through ground loops. For these reasons, several groups have been investigating techniques of adapting optical fiber technology to connect both the input and output signals to/from superconductor and RSFQ circuits.^{108,109}

Optical-to-Electrical Conversion – The coupling of optical signals (either analog or digital) into electrical stimulus for a RSFQ circuit can be accomplished using either PIN diodes or MSM diodes. MSM diodes are easily fabricated in a standard Nb superconductor IC fabrication process, since Si substrates are typically used a mechanical supports for the thin-film Josephson circuits. Alternatively, PIN diodes (made from InGaAs or GaAs) can be used either in bare chip form, or completely packaged with fiber optic connectors. InGaAs photodiodes have been operated at up to 4 GHz at 4.2 K and Si MSM diodes have been run up to 6 GHz at these temperatures. Beneficially, the performance of these devices increases as the operating temperature is reduced. In either case, care must be taken in affecting the transition from the optical device to co-planar

waveguide in order to make the electrical connection to the RSFQ circuit. In the case of off-the-shelf photodiodes, their packaging capacitance will limit the overall speed to the system.



Fig. 33 (left) Schematic of a typical optically-coupled RSFQ system. (Photo courtesy Conductus, Inc.) (right) Low-speed RSFQ shift register (of the type described in section 3.2.2) operating with both fiber optic input and fiber optic output. An integrated MSM diode is used at the input (E/O) and a laser diode is modulated by the circuit's amplified voltage output (O/E).

Electrical-to-Optical Conversion – To optically couple the RSFQ output signal from the cryogenic environment to room temperature, several methods have been studied. These include: the use of electro-optic crystals (such as Lithium Niobate or Lithium Tantalate)^{110,111} to phase modulate an incoming light beam, Mach-Zender modulators, or the direct modulation of laser diodes or light emitting diodes. Laser diodes are generally preferred to light emitting diodes on the basis of their electrical-optical slope efficiency; however, off-the-shelf laser diodes often show signs of carrier freeze-out when cooled to temperatures near 5 K.

4.3 Multi-chip modules and cryopackages

Whereas many semiconductor chips are bonded into individual packages suitable for placement on a PCB, RSFQ systems can be thought of as being interconnected with each other on a superconducting multi-chip module that resides in a "cryopackage". It is this cryopackage that a system-user mounts on a small refrigerator in order to apply cooling and power, and make all I/O connections.

4.3.1 Multi-chip modules

Building on work done in the late 1970's at IBM¹¹², the idea of a superconducting multichip module (MCM) was revived in the 1980's in Japan^{113,114,115}, and independently at TRW^{116,117} in the 1990's. Today, these processes have matured and are being refined to yield even smaller inductances in the contacts.^{118,119} In fact, the bandwidth of 25-mm bump bonds is expected to exceed 100 GHz. Different substrate-conductor combinations have also been explored including Nb-on-Si, Cu-on-Si, and Cu-on-Ceramic, but Nb-on-Si remains most popular because of the ability to fabricate the MCM "carriers" in the same process as the Nb chips themselves. The Cu-on-Si and Cu-on-Ceramic, while offering low resistance at 5 K, are not superconductive. Due of the data speeds involved, it is impractical to consider transferring bits between RSFQ chips via co-axial cables in different parts of the same system. Instead, a superconductor (Nb-on-Si) MCM can be thought of as a dual of the PCB for semiconductor ICs; however, the superconductor MCM maintains the lossless, dispersionless transmission of the data between chips. Further, the Nb-on-Si arrangement offers the ability of creating active circuitry in the MCM itself. This approach allows the distribution of global clocks throughout the system, such as the LJJ oscillator and PLL in section 3.1, and enables the possibility of both synchronous and asynchronous system operation.

Fig. 34 shows the low-temperature solder-bump technique for attaching RSFQ chips onto MCM carriers. Typical bumps are 100 μ m round pads comprising ~35 nm of Ti and an adhesion/barrier layer, 400 nm of Pd as the solder-contact layer, and 50 nm of Au to prevent oxidation of the Pd. The solder is InSn, which reflows at 118°C. After reflow, the bumps collapse to a height of about 5 μ m, yielding an inductance of ~10 pH for the contact. Fig. 35 shows the appearance of a full MCM (left) with two chips on a large carrier and close-up of arrays of test bumps (right).



Fig. 34. MCM bump-bonding / solder re-flow process of TRW for superconductor ICs.



Fig. 35. (left) Flip-chip die attach type superconductor MCM with 2 chips on a carrier. (Photo courtesy J. Spargo, TRW) (right) InSn solder bumps scanning electron micrograph. (Photo courtesy A. Smith, TRW)

Essential for an effective design of chip-to-chip transmitter and receiver circuits is an accurate understanding of the intervening electrical pathway. Propagation of signals onchip is well characterized up to the off-chip transition. Along the surface of a superconductor chip, signals follow a nearly transverse electromagnetic (TEM) mode along microstrip wiring. Currents along the wiring structures are mirrored by return currents confined below the wiring. Dispersion is low, even to hundreds of GHz. In contrast, the transition off-chip requires separate, widely separated connections for signals and ground returns. Parasitic reactances in the transition greatly affect the dispersion of transiting signals. Effective bandwidths of the transitions typically range up to tens of GHz. One method of reducing the connection parasitics is to keep the physical distances of the non-microstrip pathways to an absolute minimum. The flip-chip die attach geometry excels over wire-bonding and other die attach schemes in this regard.

Although most superconductor MCM digital signal transfer schemes involve the boosting of the RSFQ signal before transmission and then recovering the SFQ pulse at the receiver, experiments have shown the direct transfer of SFQ pulses between chips on a MCM using very low-inductance bumps.¹²⁰

4.3.2 Cryopackages

Whether using a single-chip or MCM configuration, the RSFQ circuitry must be mounted in a cryopackage before mounting it on the cooling surface. In the last 10 years, much has been learned about this art.^{121,122} For reliable operation, RSFQ circuits require ambient magnetic fields of less than ~1 mG at the surface of the chip. Typically, cryopackages employ double-walled "high-µ metal" shields to provide this screening, along with a vacuum-insulated heat radiation shield. This configuration can result in a system that will reject external magnetic fields up to ~10 G and provide good thermal isolation from higher temperatures. Since the operation of RSFQ logic itself depends magnetic fields, it is possible that, as the chip is cooled below the superconducting critical temperature, stray magnetic flux quanta could become trapped (i.e. Abrikosov vortices²⁴) within a closed superconducting region in the chip ground plane. A package "defluxing" heater provides a means of getting rid of any trapped flux by raising the temperature of the chip above T_c for a short time. Ideally, a self-check procedure should monitor this effect at cool-down time and deflux the RSFQ circuits as a part of normal diagnostics.¹²³

Fig. 36 shows a demo¹²⁴ cryopackage on a cryocooler produced during an ATP program on network switching for the US Department of Commerce.¹²⁵ This package required a mounting stage at 4-5 K with a maximum power dissipation of 300 mW and a temperature stability of < 100 mK. The minimum surface area was 3.25 in. in diameter. This package maintained an ambient magnetic field < 0.5 mG, with clearance to accommodate 12 co-axial cables 0.085 OD. The second stage lifted a maximum power of 10-20 W with a minimum surface area of 20 in² and a temperature stability of 1 K. Primary concerns in the design were magnetic and electrical noise.



Fig. 36 (left) ATP program HYPRES/Boreas cryopackage/cryocooler showing all three CCR stages. The digital network switch system tested up to 4 Gb/s I/O. (right) Schematic of the CCR configuration showing the multiple temperature stages and shielding. (Photos courtesy of Conductus, Inc.)

Fig. 36(left) shows another cryopackage, designed specifically for both electrical and optical connections. This unit has been used with the high-resolution ADC described in section 2.1.1. The full ADC parallel output word was first serialized using a "shift and dump" type multiplexor on-chip (i.e. parallel-to-serial converter) and then used to modulate a serial data stream onto an optical fiber for transfer to room temperature electronics.^{126,127} Magnetic and thermal shields are shown also. Fig. 37(right) shows a similar package with 6 high-speed (>10 GHz) SMA connectors for high-speed electrical I/O. In either case, the package would be heat sunk to a cold finger on a CCR or alternatively could simply be immersion-cooled in liquid helium for development and reliability-testing.

Some applications, such as the DAC described in section 2.2.1 can benefit from the use of multiple chips, but do not necessarily require the full performance of a MCM process. The package in Fig. 38 accommodates up to 20 0.5 cm² RSFQ chips with relatively low-speed (500 MHz) interconnects. Triple high- μ metal shielding and flexible ribbon cable connectors make this design both robust and simple.



Fig. 37 (left) A cryopackage fitted for optical output with 3 high-speed lines and 18 low-speed lines and a mounting fixture for an output laser diode. (right) A similar cryopackage with 6 high-speed lines and 18 low-speed lines with dimensions: 5.75 in. x 2.1 in. x 1.1 in.



Fig. 38 Low-speed multi-chip package being developed for a Josephson AC-voltage standard (DAC).

5. Integrated RSFQ Applications

Many applications for LTS circuits have been introduced and studied.^{128,129} Some emphasizing the digital aspect of RSFQ have reached quite mature stages of development.¹³⁰ Recently, substantial funding has been made available for investigation of PetaFLOPs level computing. This future application has been extensively detailed^{131,132}, including in the companion RSFQ paper in this issue, and is therefore not covered here. Other possible applications and their cryocooler requirements are reviewed in the following sections.

5.1 Application examples

5.1.1 Pseudo-random binary sequence generators

For spread-spectrum communications protocols, it is necessary for the receiver to synchronize its internal code generator with the incoming signal before receiving data.

The speed of RSFQ can allow this synchronization to take place in only a few clock cycles, eliminating the need to send sync signals back and forth between transmitter and receiver by providing pseudo-random binary sequence generators.¹³³ Northrop Grumman has made good progress on this application.^{134,135,136}

5.1.2 Network switches

The transmission capacity of a single mode optical fiber is more than 1 Tb/s and the speed of RSFQ is well matched to the bandwidth of optical fiber. Although photons (with their low energy) are a good match for sending signals, they interact only weakly, making it difficulty to perform fully-optical switching. The optical I/O capability of RSFQ (see section 4.3.2) creates the possibility of constructing a full optical network switch.¹²³ A 2node SFQ crossbar switch has been demonstrated with both data streams over 16 Gb/s at Northrop Grumman, while a 16x16 design was demonstrated at 3 Gb/s by TRW.¹³⁷ The ATP program discussed in section 4.3.2 is another good example. Unlike purely optical switching fabrics, RSFQ data switches can be rapidly reconfigured. For instance, for the Asynchronous Transfer Mode (ATM) packet length of 53 bytes (i.e. 424 bits), it is necessary for an OC-192 data switch to configure the crosspoints every 42 ns.¹³⁸ While optical crosspoints are not fast enough for this, it is well within the capability of today's RSFQ circuits.¹³⁹ In fact, one analysis has shown that a 128x128 channel self-routing Batcher-Banyan switching core implemented in a 0.8-µm RSFQ technology could provide throughput close to 100 Gbit per channel, dissipate about 10 mW of power, and fit on a single 1-cm² die.¹⁴⁰

5.1.3 Software Defined Radio

Considerable interest has arisen in the idea of enabling software-defined radios (SDR)¹⁴¹ with RSFQ technology.¹⁴² The SDR concept relies on the digitization of communications waveforms as close to the antenna as possible, with subsequent hardware and software DSP to sort out the signals. For semiconductor ADCs, one or two stages of down-conversion and filtering are typically needed in order to bandlimit a single channel and move it to the baseband before it can be handled digitally. Using one or a combination of the approaches discussed in section 2.1, however, an entire band or several bands could be digitized at once, skipping one or all the mixing stages, while preserving signal fidelity. The ability to feed the digitized waveforms directly into an RSFQ digital pre-filter before handing off baseband signals to the control hardware might also enable dynamically programmable or software reconfigureable systems in which a single platform can simultaneously satisfy the requirements of communications, radar, and electronic warfare applications.

5.1.4 Digital RF Memories

Militaries are moving toward digital multi-function systems (as a replacement for dedicated RF systems) in order to reduce cost and increase flexibility. A digital RF Memory (DRFM) is an Electronic Countermeasure (ECM) system designed to digitize wideband waveforms, store them in a cache memory, and apply time-delays and

frequency-shifts to the data before uploading them to a direct digital synthesizer (DDS) for retransmission. The purpose of this is to put up false or distorted signals that will be misinterpreted by enemy receivers. Naturally, in order to appear realistic, the linearity of all DRFM components should be greater than the accuracy of the targeted receivers. Further, there is a requirement that all processing take place in near-realtime. RSFQ technology has demonstrated all the necessary components, including ADC, DAC, RAM, DSP, etc. for this application.



Fig 39. Digital RF memory test at KOR Electronics (San Diego, CA) showing how an existing system can be retrofitted with an RSFQ chip without loss of performance.

As a first step toward the realization of an all-RSFQ DRFM, HYPRES (Elmsford, NY) has worked with Kor Electronics (San Diego, CA) to take a traditional DRFM and replace only the ADC portion with the RSFQ ADC described in section 2.1.1. Fig. 39 shows the measurement setup for such tests. As input, a 500 ps wide pulse was applied to the ADC at a rate of 29 MHz. The digitized waveform was then passed directly from the superconductor ADC to a fast semiconductor memory and immediately uploaded to a GaAs DAC. Power spectra before ADC digitization and after conversion back to analog are shown. Performance was limited by the DAC fidelity. Although rigorous measurements are not yet complete, this demonstration proves the validity of replacing a single system section with an RSFQ component.

5.1.5 Time-to-digital converters

Another area where RSFQ circuits are particularly well suited is for the instrumentation of high-energy physics (HEP) experiments.¹⁴³ In such applications, LHe is typically used to cool superconducting magnets, creating a natural place for cooling the circuits. Because RSFQ circuits are inherently radiation-hard^{144,145}, they perform well in high-radiation HEP environments. Further, such circuits offer better sensitivity for the measurement of weak detector signals and can reduce SNR degradation by performing

the digitization and multiplexing of many detector signals before the transition to room temperature. A Time-to-Digital Converter (TDC) is one such detector that can be made using RSFQ technology. A TDC is essentially an electronic stopwatch, able to determine the absolute and relative time difference between events (or "hits") and report them as digital numbers.



Fig. 40. (left) 8-channel TDC chip and (right) block diagram of a single channel.

Fig. 40 shows the layout of an 8-channel TDC chip (left) and block diagram of a single-channel (right). Each TDC channel consists of a 14-bit RSFQ counter based on T flip-flops with destructive readouts, a 9-hit (i.e. 9-word) shift register-based FIFO memory, and a parallel-to-serial converter with output driver. To facilitate both external user control and data output from the TDC, a complete VXI-bus user interface with LabView control software has also been constructed. A detailed design of the RSFQ multi-hit TDC circuit is described in Refs. 146 and 147. Interestingly, the binary counter is the only component required to operate at the maximum GHz rate. The FIFO buffer is used to store multiple time stamps associated with different input hits and the parallel-toserial converter provides a serial mode of data readout. An extra "valid bit" register has even been added to provide tagging capabilities in order to distinguish between valid information and time references, blank time stamps, etc. As shown on the measurement in Fig. 41(left), the applied distance between the first and the second hits is $0.2000 \,\mu s$ and the clock frequency is 33 GHz. The 13-bit binary data output is (1100110111111), which is 6591 in decimal representation. Thus, $6591 \times (1/33 \text{ GHz}) = 0.1997 \ \mu\text{s} = 0.2 \ \mu\text{s} \pm 2.5 \ \text{ps}$, as dictated by the design. Further applications are discussed in Ref. 148. Fig. 41(right) shows a prototype control station for the TDC instrument currently under development by HYPRES (Elmsford, NY) for the US Department of Energy's Fermilab (Batavia, IL).



Fig. 41 (left) High-speed testing of the digital (coarse) part of the TDC showing 2.5 ps resolution and (right) TDC user interface showing a VXI crate with interface cards and controlling PC with LabVIEW acquisition, control, and display software.

5.1.6 Digital signal autocorrelators

Signal autocorrelators perform a correlation function on a spectrum to detect the presence of periodic signals, even when the signal strength is very weak. This is based on the principle that random noise (non-periodic) averages down and signals (periodic) are brought out. Unfortunately, typical semiconductor-based systems can take msec to seconds to reveal the presence of some covert communications waveforms or to receive spread-spectrum communications signals in areas with significant clutter. RSFQ autocorrelators offer two important advantages over other technologies. First, the hardware complexity of a broadband digital correlator decreases rapidly with clock speed. From this consideration, RSFQ digital correlators running at 20 GHz clock speeds definitely outperform the existing analog correlators when the level of ~100 stages (or "lags") is reached. With ~1000 lags they will beat the digital as well as the (very complex and costly) analog-digital systems. Another advantage of an RSFQ correlator arises in space-borne applications where reduction in power dissipation could be of crucial importance. Power dissipated by an RSFQ correlator can be reduced to below 1 μ W (at 4.2 K) per channel for clock speeds up to 20 GHz. Even with a very inefficient cryocooler (say 0.1%) this translates into only 1 mW per channel at room temperature and is two orders of magnitude better than semiconductor correlators.

The basic correlation process consists of a standard sum of products calculation. Given two data vectors, the corresponding elements from each vector are multiplied and then all the products are summed to a single result. One of the vectors is then shifted by a single element and the multiply and sum process is repeated to produce the next result data point. This process is illustrated in Fig. 42(right). A 16-channel, 4 GHz bandwidth, double oversampling (16 GHz clock), RSFQ autocorrelator of this type has been demonstrated.^{144,149} The active area of the correlator IC is shown in Fig. 42(left).



Fig. 42 (left) Mask layout for autocorrelator. (right) Block diagram of autocorrelator.

5.1.7 Fast Fourier Transform Engines

For many digital signal processing applications, especially in SIGINT (signal intercept) and Comms (communications), a transform into the frequency domain allows the use of significantly faster algorithms for discriminating, selecting, and identifying waveforms. Unfortunately, the calculation of the Fourier transform of a signal (even with the Fast Fourier Transform [FFT] method) is very compute-intensive, and grows more so as finer frequency resolution is desired. Fig. 43 shows an RSFQ Decimation-in-Time (DIT) Radix-2 Butterfly integrated circuit which is the basic cell needed to implement the 32-point Fast Fourier Transform (FFT) in a parallel data flow architecture.⁹⁷ The radix-2 butterfly circuit uses serial RSFQ math and consists of four single bit-wide serial multipliers and eight carry-save serial adders of the type outlined in section 3.3.3. The circuit with 16-bit word-length employs only 3400 JJs, occupies an area of 3.8 mm x 2.0 mm, and dissipates less than 1.1 mW power.



Fig. 43. (left) 2 Radix-2 16-bit multipliers on a 0.5 cm² chip. (right) Full operation of a radix-2 butterfly with 5-bit word length. Outputs are RTZ with LSBs first. Inputs are $\mathbf{W}_{Im} = (11111)$, $\mathbf{Y}_{Im} = (01110)$, $\mathbf{W}_{Re} = (11011)$, $\mathbf{Y}_{Re} = (10101)$, $\mathbf{X}_{Re} = -\mathbf{X}_{Im} = (1011000000)$, $\mathbf{X}_{Im} = -\mathbf{X}_{Re} = (0101000000)$. Note, no subtractors are used in the circuit.

A DIT radix-2 butterfly operation requires one complex ($\Re e \& \Im m$) multiply and two complex additions. A purely real implementation requires four real multipliers and six real adders to compute:

$$X_{Re} = X_{Re} + (Y_{Re} \cdot W_{Re} - Y_{Im} \cdot W_{Im}) \text{ and } X_{Im} = X_{Im} + (Y_{Im} W_{Re} + Y_{Re} W_{Im}),$$

$$Y_{Re} = X_{Re} - (Y_{Re} \cdot W_{Re} - Y_{Im} \cdot W_{Im}) \text{ and } Y_{Im} = X_{Im} + (Y_{Im} W_{Re} + Y_{Re} W_{Im}).$$
(3)

Fig. 43(right) shows a demonstration of full functional operation of the radix-2 butterfly chip with a 5-bit word length. To multiply, $N \ge 1$ -bit serial multipliers are used. To add/subtract, 1-bit carry-save serial adders (CSSA) are used.

5.2 Cryogenic refrigerator requirements

RSFQ circuitry must be cooled for operation. The temperature of operation is normally selected to be ~¹/₂ of the material's superconducting transition "critical temperature" (T_c). For operating temperatures below ¹/₂ T_c , superconducting parameters are not strongly sensitive to small variations in temperature. Above ¹/₂ T_c , Josephson junction device operation becomes very sensitive to thermal fluctuations, resulting in greatly reduced parameter operating margins.¹⁵⁰ For Nb ($T_c = 9.23$ K), operating at the boiling point of LHe at one atmosphere (4.2 K), meets this requirement. A closed-cycle refrigerator with a 5 K final stage temperature is also a suitable platform.¹⁵¹ At these temperatures, RSFQ circuits require ~10 to 100 mK stability.

Cooling of commercial RSFQ superconducting electronics requires low cost, closed cycle refrigeration. Logistics inhibit the widespread use of LHe, except in a laboratory setting. Space-based (satellite) applications of RSFQ require cryocoolers of the highest reliability, lowest input power, and small weight and size; while marginal capital cost relative to that of the electronics subsystem, are the paramount concern for other applications. A cost-reliability goal for commercial cryocoolers has been suggested at \$1K to 10K for a unit with a 2-10 year lifetime.¹⁵²

Refrigeration power required for a RSFQ system will likely be a few watts at most and the dominant heat load will be heat leaks by radiation and conduction from the surrounding interface electronics, rather than the RSFQ chips themselves. Consequently, the refrigeration power to go from 300 to 77 K is not much less (~30%) than to go from room temperature to 5 K. However, input power requirements are about 600-2000 W for the LTS RSFQ temperature range, for 0.5 W of refrigeration power, due to the Carnot and actual thermal cycle efficiencies.

Ultimately, it is the thermal conductivity of the I/O and the active device dissipation that determines the requirements of the cryocooler. For a typical RSFQ ADC system, a refrigerator might be needed that can cool a minimum of 250 mW at 5 K; ideally 350 mW. This cooling budget consists of: 100 mW for the RSFQ chip, 70 mW for the I/O heat load from a 40 K stage to the 5 K stage. With a 50% to 100% design margin, this results in 250 mW to 340 mW total power lift.

5.2.1 Product platforms

Most refrigerator systems have two separate mechanical components: a cold head and a compressor. The cold head is where the RSFQ circuits are mounted. It can be compact and dissipates only a small amount of power. The compressor contains a motor driven compressor stage and (in some cases) oil particle traps, and dissipates almost all of the required power. It is important to note that the power required by the compressor is for operating a motor, and thus can be primary unregulated power. The fundamentals of CCR operation can be found in Ref.153.

Since extending the lifetime of existing cryocoolers directly impacts cost, and since moving parts limit long-term reliability or lifetime, the most dramatic small cryocooler improvements are in the form of pulse tube refrigerators with only one moving part.¹⁵⁴ The pulse tube is second only to Stirling refrigerators in efficiency. Stirling coolers have gained widespread acceptance for use in infrared sensor cooling. First in reliability and second in current production today are Gifford-McMahon (GM) refrigerators, which are used as cryopumps on high vacuum systems. While these GM production units typically reach 12-15 K, high heat-capacity materials, such as Er₃Ni can be used instead of Pb in a regenerative heat exchanger to yield 4-5 K operation, without resorting to the previously required separate Joule-Thomson (JT) final stage.¹⁵⁵ Such units are expandable to lift several watts at the 5 K level by using a higher-power compressor.¹⁵⁶

With regard to CCR reliability, MTBFs of 80,000 hours are achievable with GM and JT cryocoolers, although some periodic maintenance may be required (i.e. oil adsorber replacement) perhaps every 18-24 months. Theoretical lifetimes for free-piston Stirling cryocoolers using gas bearings and/or flexture bearings or pulse-tube coolers are also of this magnitude, but do not yet have operating histories to support such numbers.¹¹⁹ Fig. 44 illustrates the myriad of platforms which can accommodate a CCR-packaged RSFQ system. Although not likely to be found on a handheld devices any time soon, solutions do exist for the majority of fixed-site and mobile platforms, with the possibility of dismounted (portable) systems in the future.

The practicality of RSFQ-based applications is linked to the ability to package and power such systems. Various options exist for active (closed-cycle refrigerator or CCR) cryocooling to the necessary 4-5 Kelvin temperatures. Today's cooling options can be loosely grouped into two classes: "Commercial" and "Developing". Examples are given in the following sections.



Fig. 44 Platforms capable of fielding cryogenic electronics.

5.2.2 Commercial Coolers

Near-term RSFQ systems can make use of commercially available cryocoolers. (i.e., no cooler development work is needed). Instead, work would focus on system integration issues, input/output, and robustness.

The Leybold "CoolPower 4.2LAB": Fig.45(left) shows this compact (19 in. rackmountable) cooler which provides a full 0.75 W at 5 K, drawing 2 kW at 220 V (singlephase) input power. It is air-cooled and requires one standard maintenance every 24 months. This 2-stage Gifford-McMahon (GM) cycle CCR is used for the HYPRES primary voltage standard product and is currently deployed, in the field, as a platform for superconductor ICs. The < 100 kg. unit has not been optimized for size and might be reduced in overall profile without undue impact on performance.



Fig. 45 (left) A 19 in. rack-mountable Leybold "4.2LAB" 2-stage Gifford-McMahon cryocooler delivering ¹/₄ W of lift at 4 K for 2 kW input power. (right) A CTI single stage Gifford-McMahon cryocooler delivering 60 W lift at 60 K with a no-load temperature of 45 K.

The CTI "Cryodyne" Refrigerator: Fig.45(right) shows a single stage GM cooler based on the CTI M350 and 8F Cryopumps which delivers 6 W of lift at 60 K using 600 W from the wall.¹¹⁹ A second stage might be added to the cold-head to achieve the required specifications, perhaps even with the same compressor. Many of these units are currently deployed in the field as a platform for Conductus superconductor HTS filters and have demonstrated excellent reliability statistics. At only 60 lbs., this cooler easily mounts into a standard half-ATR rack and is gaining acceptance within the wireless base-station community as a communications platform. Other 4-5 K commercial cryocoolers are available from many different manufacturers including APD Cryogenics, Sumitomo, Toshiba, Mitsubishi, etc. Improved high-capacity versions (suitable for ground base or large shipboard installations) have recently entered the market as well.

5.2.3. Developing Coolers

The reduction in form-factor necessary to realize a single-person-portable or "backpack"sized system stems from currently demonstrated (but not yet commercial) technology. There are several promising candidates for 4-5 K RSFQ cooling, although none has yet been demonstrated with the necessary specifications.

The TRW 3503 Pulse-tube cooler:¹⁵⁷ Fig.46(left) shows this ultra-rugged unit which contains no moving parts at the cold-head and has been space-qualified. (Two units are currently deployed in satellites). The unit provides 0.3 W of lift at 35 K for 82 W into the compressor with a 300 K sink temperature: weight = 12.1 kg, size = 341 mm \times 200 mm \times 498 mm. Additional study into the use of rare-earth regenerators and or a JT expansion stage in the design is the focus of work needed to explore the possibility of 5 K operation. The clever use of reciprocating flexture bearings in the Stirling compressor allows for very little net vibration in the unit, a good match for the requirements of satellite systems.



Fig. 46 (left) Space-qualified TRW 3503 Pulse-tube cryocooler with Sterling compressor reaches 35 K today. (right) Example of a full-custom "MMS 50-80K" class split-sterling cooler for space applications reaches which reaches 4.5 K.

The Matra Marconi Space "MMS 50-80K" class of split-Stirling cryocoolers:¹⁵⁸ Fig. 46(right) shows another custom unit designed for ultra-long life applications for the European Space Agency (ESA). The 18 kg unit shown can be pushed down to provide 0.11 W of lift at 4.5 K from a compressor power budget of 145 W. Further optimization

has been suggested to increase the lift capacity; however, the cost-to-produce may remain very high, even in large quantities.

The recent introduction of off-the-shelf 5 K CCRs, such as the Leybold unit in section 5.2.2, has already resulted in Nb superconductor IC-based products being brought to market. The HYPRES Primary Josephson Voltage Standard (see Fig. 47), previously available only in a LHe-dewar format, is now being sold as a fully self-contained unit based on this CCR. Besides the long-term savings in cryogens for the user, the upgraded unit now requires less maintenance. Further reductions in the size-weight-power profile of CCRs will undoubtedly open up further markets as outlined in section 5.1. The lack of application pull has slowed this development more than the technical challenges. Simply put, if there is a market for cryogenic refrigeration, it could soon be available with the same reliability and cost/performance as household refrigerators.



Fig. 47 Availability of off-the-shelf cryogenic refrigerators has made superconductor IC-based products much more user-friendly. This fully self-contained commercial Primary Voltage Standard system from HYPRES uses an Nb trilayer superconductor IC with an array of over 20,000 JJs to reproduce the *Systeme Internationale* (SI) unit of the Volt for metrology applications in any lab.

6. Conclusion

As we move closer to the centennial celebration of the 1911 discovery of the phenomenon of superconductivity, the prospect of practical and useful applications of superconductor microelectronics is at its most promising. Fifty years of superconductor research into first analog and then digital circuits has developed in the shadow of a semiconductor-fueled "information revolution" which has invigorated economies and shaped cultures. Exploiting the massive investment in semiconductor integrated circuit

processing equipment, design techniques, and application niches, the very demand for "100 GHz-level" performance created by *semiconductors* may, in fact, only be fulfilled by *superconductors*. RSFQ technology could be the key. ¹⁵⁹

RSFQ data converters are the fastest and most sensitive ever demonstrated. With a full cadre of clocking, logic, and memory approaches under development, this versatile technology could conceivably merge the Digital and RF domains, once and for all. Moreover, as quantum computation, optical and biological systems, or other new technologies mature, RSFQ may be the only approach with the speed and integration scale to bridge the gap between traditional electronic data and future formats.

The key hurdle to achieving these technical goals is one of investment – in both people and facilities. The US DoD "University Research Initiative" in LTS Digital Electronics that ran from 1992 – 1997 produced a number of new academic design centers for RSFQ. If this technology is to continue to mature, these centers must be allowed to thrive. Moreover, the inclusion the cooling and interface components requires that cryogenics experts become a standard part of the RSFQ system design team. System form factor, refrigeration power, and operating temperature variations need to be well defined; heat leaks and magnetic shielding are key constraints for system packaging. But these are quite solvable issues. Indeed, with proper investment, prototype RSFQ systems for wireless base-station receivers and network switches could be available within 2-3 years. In the end, the cryogenic nature of RSFQ systems will not be as much a technological issue, as a psychological issue for the prospective user – it represents a true paradigm shift in the definition of an electronic system. The desire for 100 GHz performance, however, if great enough, can surmount even this barrier.

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